

For online information and ordering of this and other Manning books, please visit www.manning.com. The publisher offers discounts on this book when ordered in quantity. For more information, please contact

Special Sales Department
Manning Publications Co.
20 Baldwin Road
PO Box 261
Shelter Island, NY 11964 Email: orders@manning.com

©2011 by Manning Publications Co. All rights reserved.

No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by means electronic, mechanical, photocopying, or otherwise, without prior written permission of the publisher.

Many of the designations used by manufacturers and sellers to distinguish their products are claimed as trademarks. Where those designations appear in the book, and Manning Publications was aware of a trademark claim, the designations have been printed in initial caps or all caps.

Recognizing the importance of preserving what has been written, it is Manning's policy to have the books we publish printed on acid-free paper, and we exert our best efforts to that end. Recognizing also our responsibility to conserve the resources of our planet, Manning books are printed on paper that is at least 15 percent recycled and processed without the use of elemental chlorine.

Manning Publications Co. 20 Baldwin Road PO Box 261 Shelter Island, NY 11964 Development editor: Sebastian Stirling Copyeditor: Liz Welch Typesetter: Composure Graphics Cover designer: Marija Tudor

ISBN: 9781935182399 Printed in the United States of America 1 2 3 4 5 6 7 8 9 10 – MAL – 16 15 14 13 12 11

# brief contents

Part I	GETTING STARTED				
	1 •	Introduction to R 3			
	2	Creating a dataset 21			
	3	Getting started with graphs 45			
	4	Basic data management 73			
	5	Advanced data management 91			
PART II	<b>BASIC METHODS</b> 117				
	6	Basic graphs 119			
	7	Basic statistics 141			
Part III	Int	ERMEDIATE METHODS171			
	8	Regression 173			
	9 -	Analysis of variance 219			
	10	Power analysis 246			
	11 •	Intermediate graphs 263			
	12	Resampling statistics and bootstrapping 291			

Part IV	ADVANCED METHODS311
	13 • Generalized linear models 313
	14 Principal components and factor analysis 331
	15 • Advanced methods for missing data 352
	16 • Advanced graphics 373

# Interme<mark>d</mark>iate graphs

# This chapter covers

- Visualizing bivariate and multivariate relationships
- Working with scatter and line plots
- Understanding correlograms
- Using mosaic and association plots

In chapter 6 (basic graphs), we considered a wide range of graph types for displaying the distribution of single categorical or continuous variables. Chapter 8 (regression) reviewed graphical methods that are useful when predicting a continuous outcome variable from a set of predictor variables. In chapter 9 (analysis of variance), we considered techniques that are particularly useful for visualizing how groups differ on a continuous outcome variable. In many ways, the current chapter is a continuation and extension of the topics covered so far.

In this chapter, we'll focus on graphical methods for displaying relationships between two variables (bivariate relationships) and between many variables (multivariate relationships). For example:

- What's the relationship between automobile mileage and car weight? Does it vary by the number of cylinders the car has?
- How can you picture the relationships among an automobile's mileage, weight, displacement, and rear axle ratio in a single graph?

- When plotting the relationship between two variables drawn from a large dataset (say 10,000 observations), how can you deal with the massive overlap of data points you're likely to see? In other words, what do you do when your graph is one big smudge?
- How can you visualize the multivariate relationships among three variables at once (given a 2D computer screen or sheet of paper, and a budget slightly less than that for *Avatar*)?
- How can you display the growth of several trees over time?
- How can you visualize the correlations among a dozen variables in a single graph? How does it help you to understand the structure of your data?
- How can you visualize the relationship of class, gender, and age with passenger survival on the *Titanic*? What can you learn from such a graph?

These are the types of questions that can be answered with the methods described in this chapter. The datasets that we'll use are examples of what's possible. It's the general techniques that are most important. If the topic of automobile characteristics or tree growth isn't interesting to you, plug in your own data!

We'll start with scatter plots and scatter plot matrices. Then, we'll explore line charts of various types. These approaches are well known and widely used in research. Next, we'll review the use of correlograms for visualizing correlations and mosaic plots for visualizing multivariate relationships among categorical variables. These approaches are also useful but much less well known among researchers and data analysts. You'll see examples of how you can use each of these approaches to gain a better understanding of your data and communicate these findings to others.

# 11.1 Scatter plots

As you've seen in previous chapters, scatter plots describe the relationship between two continuous variables. In this section, we'll start with a depiction of a single bivariate relationship (x versus y). We'll then explore ways to enhance this plot by superimposing additional information. Next, we'll learn how to combine several scatter plots into a scatter plot matrix so that you can view many bivariate relationships at once. We'll also review the special case where many data points overlap, limiting our ability to picture the data, and we'll discuss a number of ways around this difficulty. Finally, we'll extend the two-dimensional graph to three dimensions, with the addition of a third continuous variable. This will include 3D scatter plots and bubble plots. Each can help you understand the multivariate relationship among three variables at once.

The basic function for creating a scatter plot in R is plot(x, y), where x and y are numeric vectors denoting the (x, y) points to plot. Listing 11.1 presents an example.

#### Listing 11.1 A scatter plot with best fit lines

The resulting graph is provided in figure 11.1.

The code in listing 11.1 attaches the mtcars data frame and creates a basic scatter plot using filled circles for the plotting symbol. As expected, as car weight increases, miles per gallon decreases, though the relationship isn't perfectly linear. The abline() function is used to add a linear line of best fit, while the lowess() function is used to add a smoothed line. This smoothed line is a nonparametric fit line based on locally weighted polynomial regression. See Cleveland (1981) for details on the algorithm.

#### Basic Scatter Plot of MPG vs. Weight

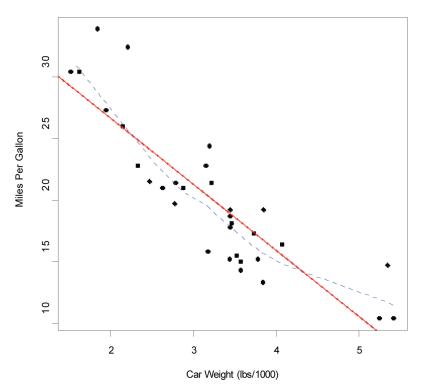


Figure 11.1 Scatter plot of car mileage versus weight, with superimposed linear and lowess fit lines.

**NOTE** R has two functions for producing lowess fits: lowess() and loess(). The loess() function is a newer, formula-based version of lowess() and is more powerful. The two functions have different defaults, so be careful not to confuse them.

The scatterplot() function in the car package offers many enhanced features and convenience functions for producing scatter plots, including fit lines, marginal box plots, confidence ellipses, plotting by subgroups, and interactive point identification. For example, a more complex version of the previous plot is produced by the following code:

Here, the scatterplot() function is used to plot miles per gallon versus weight for automobiles that have four, six, or eight cylinders. The formula mpg ~ wt | cyl indicates conditioning (that is, separate plots between mpg and wt for each level of cyl). The graph is provided in figure 11.2.

By default, subgroups are differentiated by color and plotting symbol, and separate

linear and loess lines are fit. By default, the loess fit requires five unique data points, so no smoothed fit is plotted for sixcylinder cars. The id.method option indicates that points will be identified interactively by mouse clicks, until the user selects Stop (via the Graphics context-sensitive or the Esc key. The labels option indicates that points will be identified with their row names. Here you see that the Toyota Corolla and Fiat 128 have unusually good gas mileage, given their weights. The legend.plot option adds a legend to the upper-left margin and marginal box plots

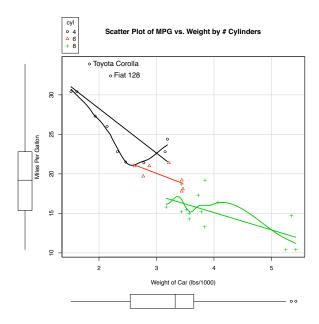


Figure 11.2 Scatter plot with subgroups and separately estimated fit lines

for mpg and weight are requested with the boxplots option. The scatterplot() function has many features worth investigating, including robust options and data concentration ellipses not covered here. See help(scatterplot) for more details.

Scatter plots help you visualize relationships between quantitative variables, two at a time. But what if you wanted to look at the bivariate relationships between automobile mileage, weight, displacement (cubic inch), and rear axle ratio? One way is to arrange these six scatter plots in a matrix. When there are several quantitative variables, you can represent their relationships in a scatter plot matrix, which is covered next.

# 11.1.1 Scatter plot matrices

There are at least four useful functions for creating scatter plot matrices in R. Analysts must love scatter plot matrices! A basic scatter plot matrix can be created with the pairs () function. The following code produces a scatter plot matrix for the variables mpg, disp, drat, and wt:

All the variables on the right of the  $\sim$  are included in the plot. The graph is provided in figure 11.3.

#### **Basic Scatterplot Matrix**

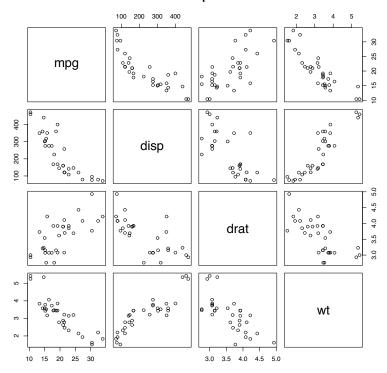


Figure 11.3 Scatter plot matrix created by the pairs() function

Here you can see the bivariate relationship among all the variables specified. For example, the scatter plot between mpg and disp is found at the row and column intersection of those two variables. Note that the six scatter plots below the principal diagonal are the same as those above the diagonal. This arrangement is a matter of convenience. By adjusting the options, you could display just the lower or upper triangle. For example, the option upper.panel=NULL would produce a graph with just the lower triangle of plots.

The scatterplotMatrix() function in the car package can also produce scatter plot matrices and can optionally do the following:

- Condition the scatter plot matrix on a factor
- Include linear and loess fit lines
- Place box plots, densities, or histograms in the principal diagonal
- Add rug plots in the margins of the cells

## Here's an example:

The graph is provided in figure 11.4. Here you can see that linear and smoothed (loess) fit lines are added by default and that kernel density and rug plots are

#### Scatterplot Matrix via car package

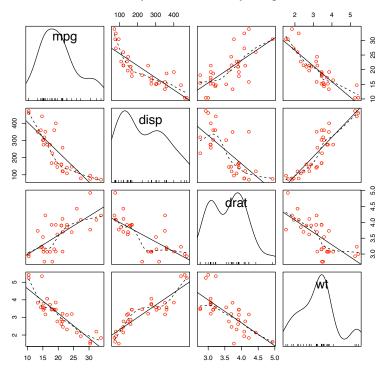


Figure 11.4
Scatter plot matrix
created with the
scatterplotMatrix()
function. The graph
includes kernel density
and rug plots in the
principal diagonal and
linear and loess fit lines.

added to the principal diagonal. The spread=FALSE option suppresses lines showing spread and asymmetry, and the lty.smooth=2 option displays the loess fit lines using dashed rather than solid lines.

As a second example of the scatterplotMatrix() function, consider the following code:

Here, you change the kernel density plots to histograms and condition the results on the number of cylinders for each car. The results are displayed in figure 11.5.

By default, the regression lines are fit for the entire sample. Including the option by .groups = TRUE would have produced separate fit lines by subgroup.

An interesting variation on the scatter plot matrix is provided by the cpairs() function in the gclus package. The cpairs() function provides options to rearrange

## Scatterplot Matrix via car package

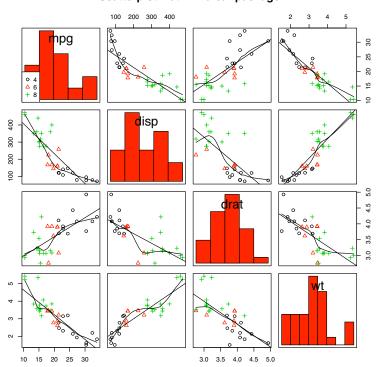


Figure 11.5 Scatter plot matrix produced by the scatterplot.Matrix() function. The graph includes histograms in the principal diagonal and linear and loess fit lines. Additionally, subgroups (defined by number of cylinders) are indicated by symbol type and color.

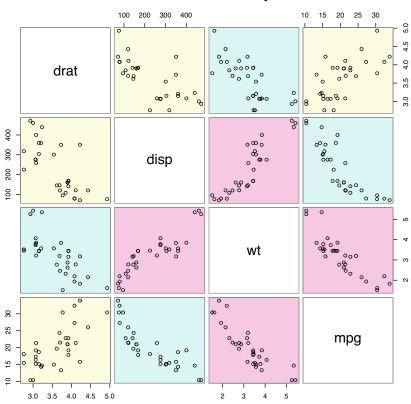
variables in the matrix so that variable pairs with higher correlations are closer to the principal diagonal. The function can also color-code the cells to reflect the size of these correlations. Consider the correlations among mpg, wt, disp, and drat:

You can see that the highest correlations are between weight and displacement (0.89) and between weight and miles per gallon (-0.87). The lowest correlation is between miles per gallon and rear axle ratio (0.68). You can reorder and color the scatter plot matrix among these variables using the code in the following listing.

Listing 11.2 Scatter plot matrix produced with the gclus package

The code in listing 11.2 uses the dmat.color(), order.single(), and cpairs() functions from the gclus package. First, you select the desired variables from the mtcars data frame and calculate the absolute values of the correlations among them. Next, you obtain the colors to plot using the dmat.color() function. Given a symmetric matrix (a correlation matrix in this case), dmat.color() returns a matrix of colors. You also sort the variables for plotting. The order.single() function sorts objects so that similar object pairs are adjacent. In this case, the variable ordering is based on the similarity of the correlations. Finally, the scatter plot matrix is plotted and colored using the new ordering (myorder) and the color list (mycolors). The gap option adds a small space between cells of the matrix. The resulting graph is provided in figure 11.6.

You can see from the figure that the highest correlations are between weight and displacement and weight and miles per gallon (red and closest to the principal diagonal). The lowest correlation is between rear axle ratio and miles per gallon



# Variables Ordered and Colored by Correlation

Figure 11.6 Scatter plot matrix produced with the cpairs() function in the gclus package. Variables closer to the principal diagonal are more highly correlated.

(yellow and far from the principal diagonal). This method is particularly useful when many variables, with widely varying inter-correlations, are considered. You'll see other examples of scatter plot matrices in chapter 16.

# 11.1.2 High-density scatter plots

When there's a significant overlap among data points, scatter plots become less useful for observing relationships. Consider the following contrived example with 10,000 observations falling into two overlapping clusters of data:

```
set.seed(1234)
n <- 10000
c1 <- matrix(rnorm(n, mean=0, sd=.5), ncol=2)
c2 <- matrix(rnorm(n, mean=3, sd=2), ncol=2)
mydata <- rbind(c1, c2)
mydata <- as.data.frame(mydata)
names(mydata) <- c("x", "y")</pre>
```

#### Scatter Plot with 10,000 Observations

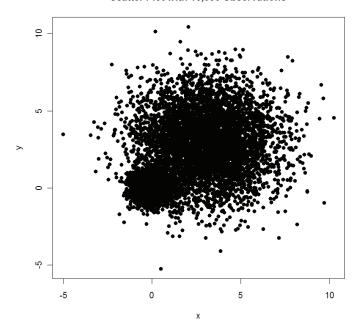


Figure 11.7 Scatter plot with 10,000 observations and significant overlap of data points. Note that the overlap of data points makes it difficult to discern where the concentration of data is greatest.

If you generate a standard scatter plot between these variables using the following code

```
with(mydata,
     plot(x, y, pch=19, main="Scatter Plot with 10,000 Observations"))
```

you'll obtain a graph like the one in figure 11.7.

The overlap of data points in figure 11.7 makes it difficult to discern the relationship between x and y. R provides several graphical approaches that can be used when this occurs. They include the use of binning, color, and transparency to indicate the number of overprinted data points at any point on the graph.

The  ${\tt smoothScatter}$  () function uses a kernel density estimate to produce smoothed color density representations of the scatterplot. The following code

Using a different approach, the hexbin() function in the hexbin package provides bivariate binning into hexagonal cells (it looks better than it sounds). Applying this function to the dataset

```
library(hexbin)
with(mydata, {
    bin <- hexbin(x, y, xbins=50)
    plot(bin, main="Hexagonal Binning with 10,000 Observations")
    })</pre>
```

#### Scatterplot Colored by Smoothed Densities

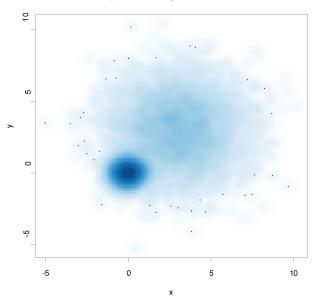


Figure 11.8 Scatterplot using smoothScatter() to plot smoothed density estimates. Densities are easy to read from the graph.

you get the scatter plot in figure 11.9.

Finally, the iplot() function in the IDPmisc package can be used to display density (the number of data points at a specific spot) using color. The code

```
library(IDPmisc)
with(mydata,
    iplot(x, y, main="Image Scatter Plot with Color Indicating Density"))
produces the graph in figure 11.10.
```

#### Hexagonal Binning with 10,000 Observations

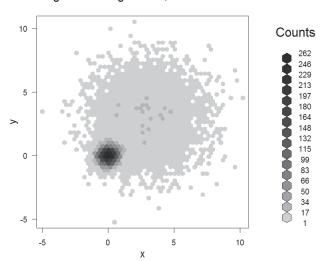


Figure 11.9 Scatter plot using hexagonal binning to display the number of observations at each point. Data concentrations are easy to see and counts can be read from the legend.

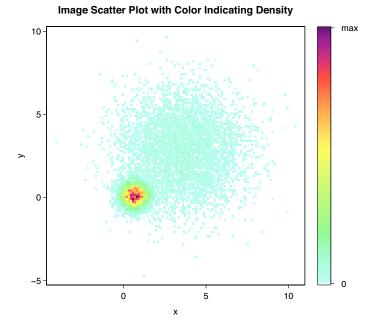


Figure 11.10 Scatter plot of 10,000 observations, where density is indicated by color. The data concentrations are easily discernable.

It's useful to note that the smoothScatter() function in the base package, along with the ipairs() function in the IDPmisc package, can be used to create readable scatter plot matrices for large datasets as well. See ?smoothScatter and ?ipairs for examples.

# 11.1.3 3D scatter plots

Scatter plots and scatter plot matrices display bivariate relationships. What if you want to visualize the interaction of three quantitative variables at once? In this case, you can use a 3D scatter plot.

For example, say that you're interested in the relationship between automobile mileage, weight, and displacement. You can use the scatterplot3d() function in the scatterplot3d package to picture their relationship. The format is

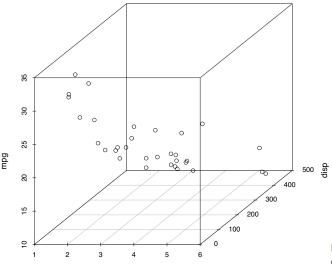
```
scatterplot3d(x, y, z)
```

where x is plotted on the horizontal axis, y is plotted on the vertical axis, and z is plotted in perspective. Continuing our example

```
library(scatterplot3d)
attach(mtcars)
scatterplot3d(wt, disp, mpg,
    main="Basic 3D Scatter Plot")
```

produces the 3D scatter plot in figure 11.11.

#### **Basic 3D Scatterplot**



wt

Figure 11.11 3D scatter plot of miles per gallon, auto weight, and displacement

The scatterplot3d() function offers many options, including the ability to specify symbols, axes, colors, lines, grids, highlighting, and angles. For example, the code

produces a 3D scatter plot with highlighting to enhance the impression of depth, and vertical lines connecting points to the horizontal plane (see figure 11.12).

As a final example, let's take the previous graph and add a regression plane. The necessary code is:

The resulting graph is provided in figure 11.13.

#### 3D Scatterplot with Vertical Lines

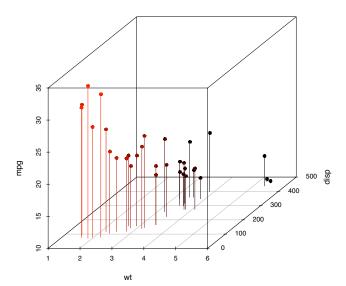


Figure 11.12 3D scatter plot with vertical lines and shading

The graph allows you to visualize the prediction of miles per gallon from automobile weight and displacement using a multiple regression equation. The plane represents the predicted values, and the points are the actual values. The vertical distances from the plane to the points are the residuals. Points that lie above the plane are underpredicted, while points that lie below the line are over-predicted. Multiple regression is covered in chapter 8.

#### 3D Scatter Plot with Verical Lines and Regression Plane

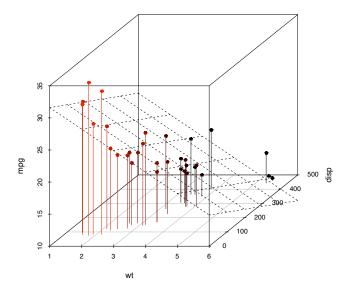


Figure 11.13 3D scatter plot with vertical lines, shading, and overlaid regression plane

#### **SPINNING 3D SCATTER PLOTS**

Three-dimensional scatter plots are much easier to interpret if you can interact with them. R provides several mechanisms for rotating graphs so that you can see the plotted points from more than one angle.

For example, you can create an interactive 3D scatter plot using the plot3d() function in the rgl package. It creates a spinning 3D scatter plot that can be rotated with the mouse. The format is

```
plot3d(x, y, z)
```

where x, y, and z are numeric vectors representing points. You can also add options like col and size to control the color and size of the points, respectively. Continuing our example, try the code

```
library(rg1)
attach(mtcars)
plot3d(wt, disp, mpq, col="red", size=5)
```

You should get a graph like the one depicted in figure 11.14. Use the mouse to rotate the axes. I think that you'll find that being able to rotate the scatter plot in three dimensions makes the graph much easier to understand.

You can perform a similar function with the scatter3d() in the Rcmdr package:

```
library(Rcmdr)
attach(mtcars)
scatter3d(wt, disp, mpg)
```

The results are displayed in figure 11.15.

The scatter3d() function can include a variety of regression surfaces, such as linear, quadratic, smooth, and additive. The linear surface depicted is the default. Additionally, there are options for interactively identifying points. See help(scatter3d) for more details. I'll have more to say about the Rcmdr package in appendix A.

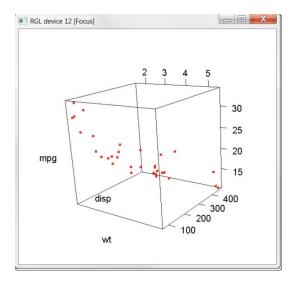


Figure 11.14 Rotating 3D scatter plot produced by the plot3d() function in the rgl package

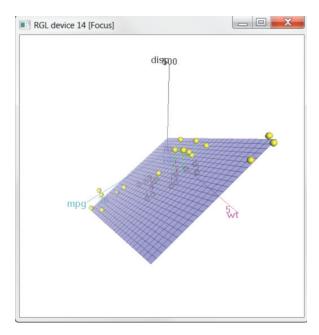


Figure 11.15 Spinning 3D scatter plot produced by the scatter3d() function in the Remdr package

#### 11.1.4 Bubble plots

In the previous section, you displayed the relationship between three quantitative variables using a 3D scatter plot. Another approach is to create a 2D scatter plot and use the size of the plotted point to represent the value of the third variable. This approach is referred to as a *bubble plot*.

You can create a bubble plot using the symbols() function. This function can be used to draw circles, squares, stars, thermometers, and box plots at a specified set of (x, y) coordinates. For plotting circles, the format is

```
symbols(x, y, circle=radius)
```

where x and y and radius are vectors specifying the x and y coordinates and circle radiuses, respectively.

You want the areas, rather than the radiuses of the circles, to be proportional to the values of a third variable. Given the formula for the radius of a circle  $(r = \sqrt{\frac{\Lambda}{\pi}})$  the proper call is

```
symbols(x, y, circle=sqrt(z/pi))
```

where z is the third variable to be plotted.

Let's apply this to the mtcars data, plotting car weight on the x-axis, miles per gallon on the y-axis, and engine displacement as the bubble size. The following code

```
main="Bubble Plot with point size proportional to displacement",
    ylab="Miles Per Gallon",
    xlab="Weight of Car (lbs/1000)")
text(wt, mpg, rownames(mtcars), cex=0.6)
detach(mtcars)
```

produces the graph in figure 11.16. The option inches is a scaling factor that can be used to control the size of the circles (the default is to make the largest circle 1 inch). The text() function is optional. Here it is used to add the names of the cars to the plot. From the figure, you can see that increased gas mileage is associated with both decreased car weight and engine displacement.

In general, statisticians involved in the R project tend to avoid bubble plots for the same reason they avoid pie charts. Humans typically have a harder time making judgments about volume than distance. But bubble charts are certainly popular in the business world, so I'm including them here for completeness.

I've certainly had a lot to say about scatter plots. This attention to detail is due, in part, to the central place that scatter plots hold in data analysis. While simple, they can help you visualize your data in an immediate and straightforward manner, uncovering relationships that might otherwise be missed.

#### Bubble Plot with point size proportional to displacement

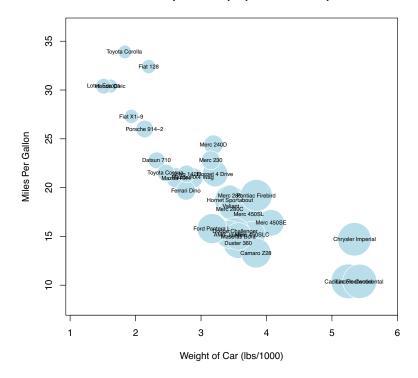


Figure 11.16 Bubble plot of car weight versus mpg where point size is proportional to engine displacement

#### 11.2 Line charts

If you connect the points in a scatter plot moving from left to right, you have a line plot. The dataset Orange that come with the base installation contains age and circumference data for five orange trees. Consider the growth of the first orange tree, depicted in figure 11.17. The plot on the left is a scatter plot, and the plot on the right is a line chart. As you can see, line charts are particularly good vehicles for conveying change.

The graphs in figure 11.17 were created with the code in the following listing.

# Listing 11.3 Creating side-by-side scatter and line plots

You've seen the elements that make up this code in chapter 3, so I won't go into details here. The main difference between the two plots in figure 11.17 is produced by the option type="b". In general, line charts are created with one of the following two functions

```
plot(x, y, type=)
lines(x, y, type=)
```

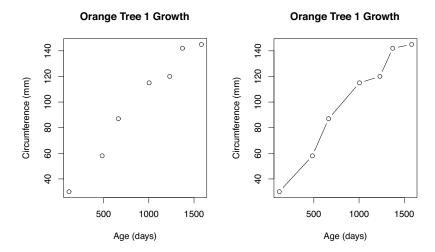


Figure 11.17 Comparison of a scatter plot and a line plot

Line charts 281

where x and y are numeric vectors of (x,y) points to connect. The option type= can take the values described in table 11.1.

Table 11.1 Line chart options

Туре	What is plotted		
p	Points only		
1	Lines only		
0	Over-plotted points (that is, lines overlaid on top of points)		
b, c	Points (empty if c) joined by lines		
s, S	Stair steps		
h	Histogram-line vertical lines		
n	Doesn't produce any points or lines (used to set up the axes for later commands)		

Examples of each type are given in figure 11.18. As you can see, type="p" produces the typical scatter plot. The option type="b" is the most common for line charts. The difference between b and c is whether the points appear or gaps are left instead. Both type="s" and type="S" produce stair steps (step functions). The first runs, then rises, whereas the second rises, then runs.

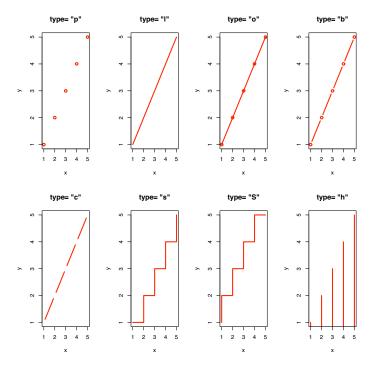


Figure 11.18 type= options in the plot() and lines() functions

There's an important difference between the plot() and lines() functions. The plot() function will create a new graph when invoked. The lines() function *adds* information to an existing graph but *can't* produce a graph on its own.

Because of this, the lines() function is typically used after a plot() command has produced a graph. If desired, you can use the type="n" option in the plot() function to set up the axes, titles, and other graph features, and then use the lines() function to add various lines to the plot.

To demonstrate the creation of a more complex line chart, let's plot the growth of all five orange trees over time. Each tree will have its own distinctive line. The code is shown in the next listing and the results in figure 11.19.

Listing 11.4 Line chart displaying the growth of five orange trees over time

```
Orange$Tree <- as.numeric(Orange$Tree)</pre>
                                                              \triangleleft
                                                                      Convert factor
ntrees <- max(Orange$Tree)</pre>
                                                                      to numeric for
                                                                      convenience
xrange <- range(Orange$age)</pre>
yrange <- range(Orange$circumference)</pre>
plot(xrange, yrange,
     type="n",
     xlab="Age (days)",
                                                                     Set up plot
     vlab="Circumference (mm)"
 )
colors <- rainbow(ntrees)</pre>
linetype <- c(1:ntrees)</pre>
plotchar <- seq(18, 18+ntrees, 1)
for (i in 1:ntrees) {
    tree <- subset(Orange, Tree==i)</pre>
    lines(tree$age, tree$circumference,
           type="b",
           1wd=2,
                                                                     Add lines
           lty=linetype[i],
           col=colors[i],
           pch=plotchar[i]
    )
}
title("Tree Growth", "example of line plot")
legend(xrange[1], yrange[2],
       1:ntrees,
       cex=0.8,
        col=colors,
                                                                     Add legend
        pch=plotchar,
        lty=linetype,
        title="Tree"
```

Correlograms 283



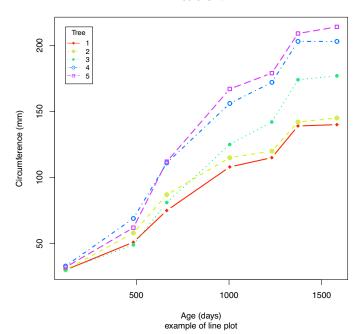


Figure 11.19 Line chart displaying the growth of five orange trees

In listing 11.4, the plot() function is used to set up the graph and specify the axis labels and ranges but plots no actual data. The lines() function is then used to add a separate line and set of points for each orange tree. You can see that tree 4 and tree 5 demonstrated the greatest growth across the range of days measured, and that tree 5 overtakes tree 4 at around 664 days.

Many of the programming conventions in R that I discussed in chapters 2, 3, and 4 are used in listing 11.4. You may want to test your understanding by working through each line of code and visualizing what it's doing. If you can, you are on your way to becoming a serious R programmer (and fame and fortune is near at hand)! In the next section, you'll explore ways of examining a number of correlation coefficients at once.

# 11.3 Correlograms

Correlation matrices are a fundamental aspect of multivariate statistics. Which variables under consideration are strongly related to each other and which aren't? Are there clusters of variables that relate in specific ways? As the number of variables grow, such questions can be harder to answer. Correlograms are a relatively recent tool for visualizing the data in correlation matrices.

It's easier to explain a correlogram once you've seen one. Consider the correlations among the variables in the mtcars data frame. Here you have 11 variables, each measuring some aspect of 32 automobiles. You can get the correlations using the following code:

<sup>&</sup>gt; options(digits=2)

<sup>&</sup>gt; cor(mtcars)

```
cyl disp
      mpg
                        hp
                             drat
                                    wt
                                         gsec
                                                VS
                                                       am
                                                           gear
                                                                  carb
     1.00 -0.85 -0.85 -0.78
                           0.681 -0.87 0.419 0.66 0.600 0.48 -0.551
    -0.85 1.00
                0.90
                     0.83 -0.700 0.78 -0.591 -0.81 -0.523 -0.49
disp -0.85 0.90 1.00 0.79 -0.710 0.89 -0.434 -0.71 -0.591 -0.56
    -0.78 0.83
                0.79
                      1.00 -0.449
                                  0.66 -0.708 -0.72 -0.243 -0.13
drat 0.68 -0.70 -0.71 -0.45 1.000 -0.71 0.091 0.44 0.713 0.70 -0.091
    -0.87 0.78 0.89 0.66 -0.712 1.00 -0.175 -0.55 -0.692 -0.58
gsec 0.42 -0.59 -0.43 -0.71 0.091 -0.17 1.000 0.74 -0.230 -0.21 -0.656
     0.66 -0.81 -0.71 -0.72
                           0.440 - 0.55
                                        0.745 1.00 0.168
                                                           0.21 - 0.570
     0.60 -0.52 -0.59 -0.24  0.713 -0.69 -0.230  0.17  1.000
                                                           0.79 0.058
gear 0.48 -0.49 -0.56 -0.13 0.700 -0.58 -0.213 0.21 0.794 1.00 0.274
carb -0.55 0.53 0.39 0.75 -0.091 0.43 -0.656 -0.57 0.058
                                                           0.27 1.000
```

Which variables are most related? Which variables are relatively independent? Are there any patterns? It isn't that easy to tell from the correlation matrix without significant time and effort (and probably a set of colored pens to make notations).

You can display that same correlation matrix using the corrgram() function in the corrgram package (see figure 11.20). The code is:

To interpret this graph, start with the lower triangle of cells (the cells below the principal diagonal). By default, a blue color and hashing that goes from lower left to upper right represents a positive correlation between the two variables that meet at that cell. Conversely, a red color and hashing that goes from the upper left to the lower right represents a negative correlation. The darker and more saturated the color, the greater the magnitude of the correlation. Weak correlations, near zero, will appear washed out. In the current graph, the rows and columns have been reordered (using principal components analysis) to cluster variables together that have similar correlation patterns.

#### Correlogram of mtcars intercorrelations

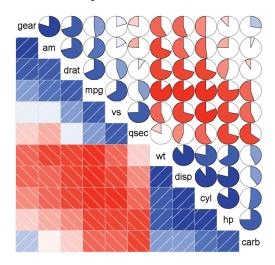


Figure 11.20 Correlogram of the correlations among the variables in the mtcars data frame. Rows and columns have been reordered using principal components analysis.

You can see from shaded cells that gear, am, drat, and mpg are positively correlated with one another. You can also see that wt, disp, cyl, hp, and carb are positively correlated with one another. But the first group of variables is negatively correlated with the second group of variables. You can also see that the correlation between carb and am is weak, as is the correlation between vs and gear, vs and am, and drat and gsec.

The upper triangle of cells displays the same information using pies. Here, color plays the same role, but the strength of the correlation is displayed by the size of the filled pie slice. Positive correlations fill the pie starting at 12 o'clock and moving in a clockwise direction. Negative correlations fill the pie by moving in a counterclockwise direction. The format of the corregram() function is

```
corrgram(x, order=, panel=, text.panel=, diag.panel=)
```

where x is a data frame with one observation per row. When order=TRUE, the variables are reordered using a principal component analysis of the correlation matrix. Reordering can help make patterns of bivariate relationships more obvious.

The option panel specifies the type of off-diagonal panels to use. Alternatively, you can use the options lower.panel and upper.panel to choose different options below and above the main diagonal. The text.panel and diag.panel options refer to the main diagonal. Allowable values for panel are described in table 11.2.

Placement	Panel Option	Description
Off diagonal	panel.pie	The filled portion of the pie indicates the magnitude of the correlation.
	panel.shade	The depth of the shading indicates the magnitude of the correlation.
	panel.ellipse	A confidence ellipse and smoothed line are plotted.
	panel.pts	A scatter plot is plotted.
Main diagonal	panel.minmax	The minimum and maximum values of the variable are printed.
	panel.txt	The variable name is printed.

Table 11.2 Panel options for the corrgram() function

#### Let's try a second example. The code

produces the graph in figure 11.21. Here you're using smoothed fit lines and confidence ellipses in the lower triangle and scatter plots in the upper triangle.

# Correlogram of mtcars data using scatter plots and ellipses

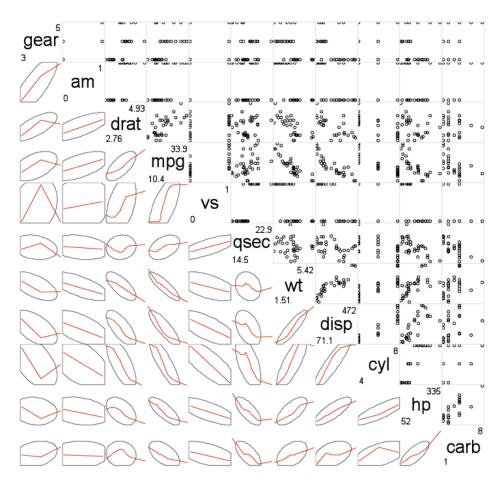


Figure 11.21 Correlogram of the correlations among the variables in the mtcars data frame. The lower triangle contains smoothed best fit lines and confidence ellipses, and the upper triangle contains scatter plots. The diagonal panel contains minimum and maximum values. Rows and columns have been reordered using principal components analysis.

## Why do the scatter plots look odd?

Several of the variables that are plotted in figure 11.21 have limited allowable values. For example, the number of gears is 3, 4, or 5. The number of cylinders is 4, 6, or 8. Both am (transmission type) and vs (V/S) are dichotomous. This explains the odd-looking scatter plots in the upper diagonal.

Always be careful that the statistical methods you choose are appropriate to the form of the data. Specifying these variables as ordered or unordered factors can serve as a useful check. When R knows that a variable is categorical or ordinal, it attempts to apply statistical methods that are appropriate to that level of measurement.

# We'll finish with one more example. The code

produces the graph in figure 11.22. Here we're using shading in the lower triangle, keeping the original variable order, and leaving the upper triangle blank.

Before moving on, I should point out that you can control the colors used by the corrgram() function. To do so, specify four colors in the colorRampPalette() function within the col.corrgram() function. Here's an example:

Try it and see what you get.

Correlograms can be a useful way to examine large numbers of bivariate relationships among quantitative variables. Because they're relatively new, the greatest challenge is to educate the recipient on how to interpret them.

To learn more, see Michael Friendly's article "Corrgrams: Exploratory Displays for Correlation Matrices," available at http://www.math.yorku.ca/SCS/Papers/corrgram.pdf.

#### Car Mileage Data (unsorted)

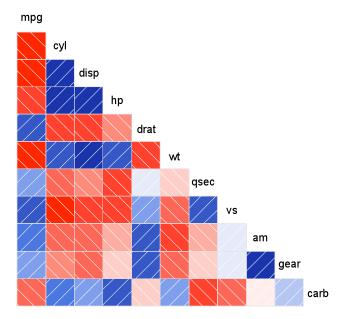


Figure 11.22 Correlogram of the correlations among the variables in the mtcars data frame. The lower triangle is shaded to represent the magnitude and direction of the correlations. The variables are plotted in their original order.

# 11.4 Mosaic plots

Up to this point, we've been exploring methods of visualizing relationships among quantitative/continuous variables. But what if your variables are categorical? When you're looking at a single categorical variable, you can use a bar or pie chart. If there are two categorical variables, you can look at a 3D bar chart (which, by the way, is not so easy to do in R). But what do you do if there are more than two categorical variables?

One approach is to use mosaic plots. In a mosaic plot, the frequencies in a multidimensional contingency table are represented by nested rectangular regions that are proportional to their cell frequency. Color and or shading can be used to represent residuals from a fitted model. For details, see Meyer, Zeileis and Hornick (2006), or Michael Friendly's Statistical Graphics page (http://datavis.ca). Steve Simon has created a good conceptual tutorial on how mosaic plots are created, available at http://www.childrensmercy.org/stats/definitions/mosaic.htm.

Mosaic plots can be created with the mosaic() function from the ved library (there's a mosaicplot() function in the basic installation of R, but I recommend you use the ved package for its more extensive features). As an example, consider the Titanic dataset available in the base installation. It describes the number of passengers who survived or died, cross-classified by their class (1st, 2nd, 3rd, Crew), sex (Male, Female), and age (Child, Adult). This is a well-studied dataset. You can see the cross-classification using the following code:

> ftable(Titanic)								
			Survived	No	Yes			
Class	Sex	Age						
1st	Male	Child		0	5			
		Adult		118	57			
	Female	Child		0	1			
		Adult		4	140			
2nd	Male	Child		0	11			
		Adult		154	14			
	Female	Child		0	13			
		Adult		13	80			
3rd	Male	Child		35	13			
		Adult		387	75			
	Female	Child		17	14			
		Adult		89	76			
Crew	Male	Child		0	0			
		Adult		670	192			
	Female	Child		0	0			
		Adult		3	20			

The mosaic () function can be invoked as

mosaic(table)

where table is a contingency table in array form, or

mosaic(formula, data=)

where formula is a standard R formula, and data specifies either a data frame or table. Adding the option shade=TRUE will color the figure based on Pearson residuals from

289

a fitted model (independence by default) and the option legend=TRUE will display a legend for these residuals.

# For example, both

```
library(vcd)
mosaic(Titanic, shade=TRUE, legend=TRUE)
and
library(vcd)
mosaic(~Class+Sex+Age+Survived, data=Titanic, shade=TRUE, legend=TRUE)
```

will produce the graph shown in figure 11.23. The formula version gives you greater control over the selection and placement of variables in the graph.

There's a great deal of information packed into this one picture. For example, as one moves from crew to first class, the survival rate increases precipitously. Most children were in third and second class. Most females in first class survived, whereas only about half the females in third class survived. There were few females in the crew, causing the Survived labels (No, Yes at the bottom of the chart) to overlap for this group. Keep looking and you'll see many more interesting facts. Remember to look at the relative widths and heights of the rectangles. What else can you learn about that night?

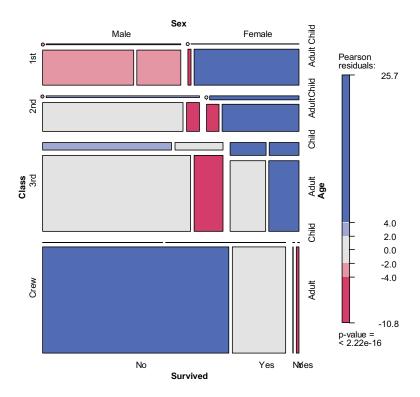


Figure 11.23 Mosaic plot describing Titanic survivors by class, sex, and age

Extended mosaic plots add color and shading to represent the residuals from a fitted model. In this example, the blue shading indicates cross-classifications that occur more often than expected, assuming that survival is unrelated to class, gender, and age. Red shading indicates cross-classifications that occur less often than expected under the independence model. Be sure to run the example so that you can see the results in color. The graph indicates that more first-class women survived and more male crew members died than would be expected under an independence model. Fewer third-class men survived than would be expected if survival was independent of class, gender, and age. If you would like to explore mosaic plots in greater detail, try running example (mosaic).

# 11.5 Summary

In this chapter, we considered a wide range of techniques for displaying relationships among two or more variables. This included the use of 2D and 3D scatter plots, scatter plot matrices, bubble plots, line plots, correlograms, and mosaic plots. Some of these methods are standard techniques, while some are relatively new.

Taken together with methods that allow you to customize graphs (chapter 3), display univariate distributions (chapter 6), explore regression models (chapter 8), and visualize group differences (chapter 9), you now have a comprehensive toolbox for visualizing and extracting meaning from your data.

In later chapters, you'll expand your skills with additional specialized techniques, including graphics for latent variable models (chapter 14), methods for visualizing missing data patterns (chapter 15), and techniques for creating graphs that are conditioned on one or more variables (chapter 16).

In the next chapter, we'll explore resampling statistics and bootstrapping. These are computer intensive methods that allow you to analyze data in new and unique ways.

# **R** IN ACTION

Robert L. Kabacoff

is a powerful language for statistical computing and graphics that can handle virtually any data-crunching task. It runs on all important platforms and provides thousands of useful specialized modules and utilities. This makes R a great way to get meaningful information from mountains of raw data.

**R** in Action is a language tutorial focused on practical problems. It presents useful statistics examples and includes elegant methods for handling messy, incomplete, and nonnormal data that are difficult to analyze using traditional methods. And statistical analysis is only part of the story. You'll also master R's extensive graphical capabilities for exploring and presenting data visually.

# What's Inside

- Practical data analysis, step by step
- Interfacing R with other software
- Using R to visualize data
- Over 130 graphs
- Eight reference appendixes

Dr. **Rob Kabacoff** is a seasoned researcher who specializes in data analysis. He has taught graduate courses in statistical programming and manages the Quick-R website at statmethods.net.

For access to the book's forum and a free ebook for owners of this book, go to manning.com/RinAction



- "Lucid and engaging ... a fun way to learn R!"
  - —Amos A. Folarin University College London
- Finally, a book that brings R to the real world.
  - Charles Malpas University of Melbourne
- R from a programmer's point of view."
  - —Philipp K. Janert Principal Value, LLC
- 66 A great balance of targeted tutorials and in-depth examples.
  - -Landon Cox, 360VL, Inc.
- "An excellent introduction and reference from the author of the best R website."
  - Christopher Williams University of Idaho



